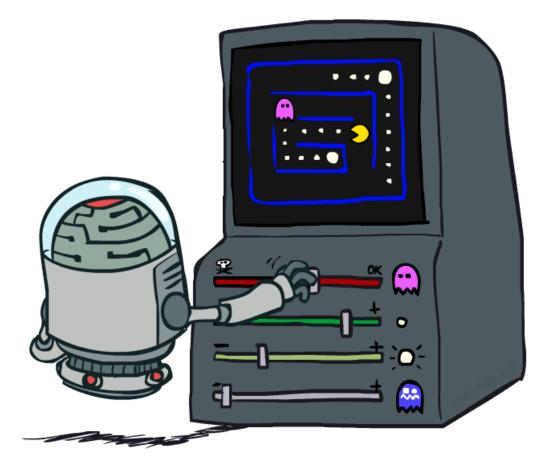
#### CSCI 446: Artificial Intelligence Reinforcement Learning II



Instructor: Michele Van Dyne

[These slides were created by Dan Klein and Pieter Abbeel for CS188 Intro to AI at UC Berkeley. All CS188 materials are available at http://ai.berkeley.edu.]

# Today

- Exploration vs Exploitation
- Approximate Q-Learning
- Q-Learning and Least Squares
  - Overfitting: Why Limiting Capacity Can Help
- Policy Search

### **Reinforcement Learning**

- We still assume an MDP:
  - A set of states s ∈ S
  - A set of actions (per state) A
  - A model T(s,a,s')
  - A reward function R(s,a,s')
- Still looking for a policy π(s)



- New twist: don't know T or R, so must try out actions
- Big idea: Compute all averages over T using sample outcomes

#### The Story So Far: MDPs and RL

Known MDP: Of	ffline Solution
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Goal	Technique
Compute V*, Q*, $\pi^*$	Value / policy iteration
Evaluate a fixed policy $\pi$	Policy evaluation

#### Unknown MDP: Model-Based

Goal	Technique
Compute V*, Q*, $\pi^*$	VI/PI on approx. MDP
Evaluate a fixed policy $\pi$	PE on approx. MDP

#### Unknown MDP: Model-Free

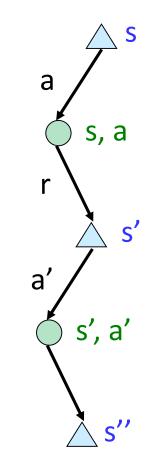
Goal	Technique
Compute V*, Q*, $\pi^*$	Q-learning
Evaluate a fixed policy $\pi$	Value Learning

#### **Model-Free Learning**

- Model-free (temporal difference) learning
  - Experience world through episodes

 $(s, a, r, s', a', r', s'', a'', r'', s'''' \dots)$ 

- Update estimates each transition (s, a, r, s')
- Over time, updates will mimic Bellman updates



## Q-Learning

We'd like to do Q-value updates to each Q-state:

$$Q_{k+1}(s,a) \leftarrow \sum_{s'} T(s,a,s') \left[ R(s,a,s') + \gamma \max_{a'} Q_k(s',a') \right]$$

- But can't compute this update without knowing T, R
- Instead, compute average as we go
  - Receive a sample transition (s,a,r,s')
  - This sample suggests

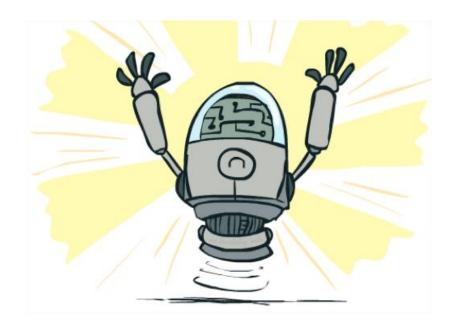
 $Q(s,a) \approx r + \gamma \max_{a'} Q(s',a')$ 

- But we want to average over results from (s,a) (Why?)
- So keep a running average

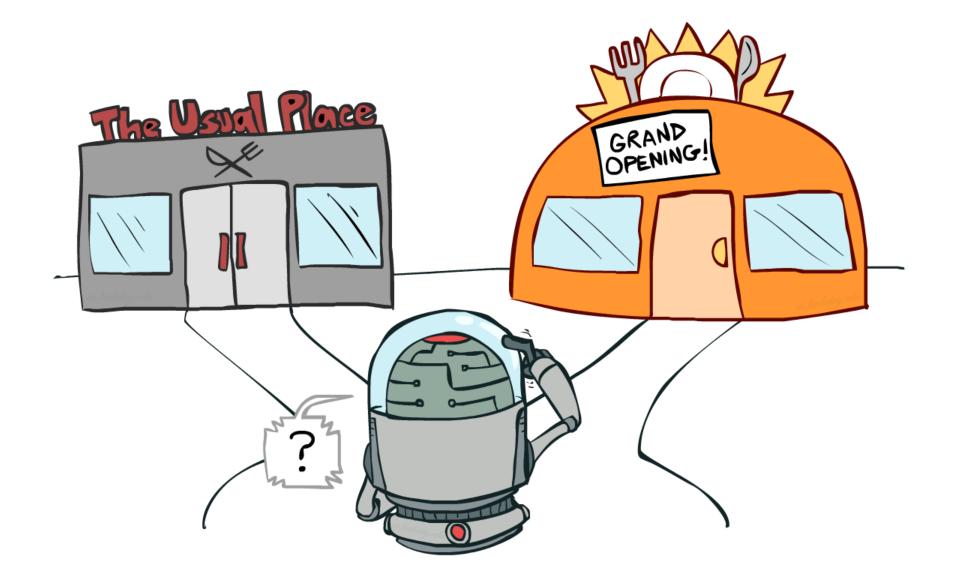
$$Q(s,a) \leftarrow (1-\alpha)Q(s,a) + (\alpha) \left[ r + \gamma \max_{a'} Q(s',a') \right]$$

## **Q-Learning Properties**

- Amazing result: Q-learning converges to optimal policy -- even if you're acting suboptimally!
- This is called off-policy learning
- Caveats:
  - You have to explore enough
  - You have to eventually make the learning rate small enough
  - ... but not decrease it too quickly
  - Basically, in the limit, it doesn't matter how you select actions (!)



#### **Exploration vs. Exploitation**



## How to Explore?

- Several schemes for forcing exploration
  - Simplest: random actions (ε-greedy)
    - Every time step, flip a coin
    - With (small) probability ε, act randomly
    - With (large) probability 1- $\varepsilon$ , act on current policy
  - Problems with random actions?
    - You do eventually explore the space, but keep thrashing around once learning is done
    - $\hfill\blacksquare$  One solution: lower  $\epsilon$  over time
    - Another solution: exploration functions



[Demo: Q-learning – manual exploration – bridge grid (L11D2)] [Demo: Q-learning – epsilon-greedy -- crawler (L11D3)]

## **Exploration Functions**

- When to explore?
  - Random actions: explore a fixed amount
  - Better idea: explore areas whose badness is not (yet) established, eventually stop exploring
- Exploration function
  - Takes a value estimate u and a visit count n, and returns an optimistic utility, e.g. f(u, n) = u + k/n



**Regular Q-Update:**  $Q(s,a) \leftarrow_{\alpha} R(s,a,s') + \gamma \max_{a'} Q(s',a')$ 

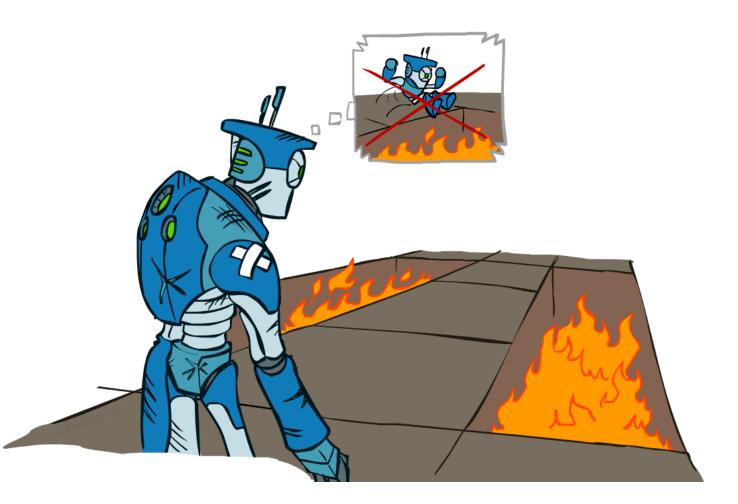
Modified Q-Update:  $Q(s,a) \leftarrow_{\alpha} R(s,a,s') + \gamma \max_{a'} f(Q(s',a'), N(s',a'))$ 

Note: this propagates the "bonus" back to states that lead to unknown states as well!

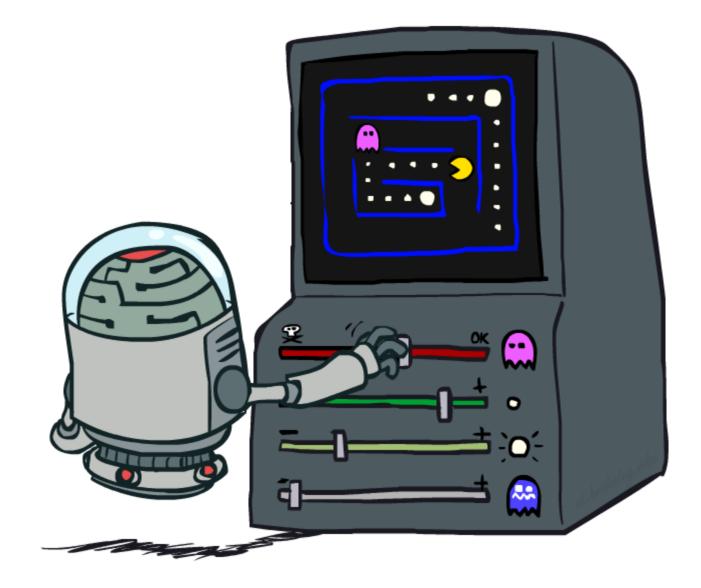
[Demo: exploration – Q-learning – crawler – exploration function (L11D4)]

## Regret

- Even if you learn the optimal policy, you still make mistakes along the way
- Regret is a measure of your total mistake cost: the difference between your (expected) rewards, including youthful suboptimality, and optimal (expected) rewards
- Minimizing regret goes beyond learning to be optimal – it requires optimally learning to be optimal
- Example: random exploration and exploration functions both end up optimal, but random exploration has higher regret

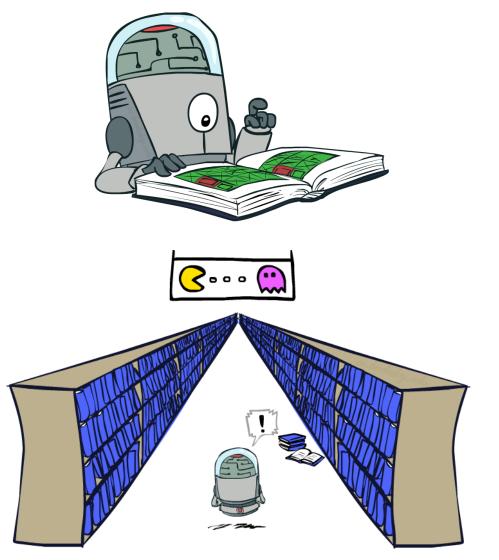


#### Approximate Q-Learning



### **Generalizing Across States**

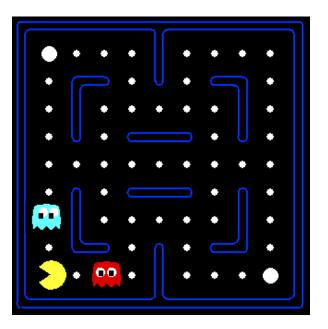
- Basic Q-Learning keeps a table of all q-values
- In realistic situations, we cannot possibly learn about every single state!
  - Too many states to visit them all in training
  - Too many states to hold the q-tables in memory
- Instead, we want to generalize:
  - Learn about some small number of training states from experience
  - Generalize that experience to new, similar situations
  - This is a fundamental idea in machine learning, and we'll see it over and over again



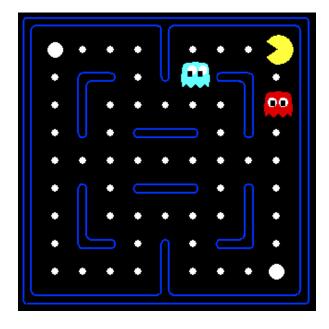
[demo – RL pacman]

#### Example: Pacman

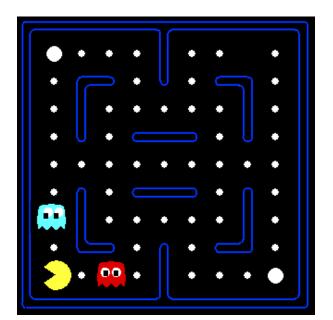
Let's say we discover through experience that this state is bad:



In naïve q-learning, we know nothing about this state:



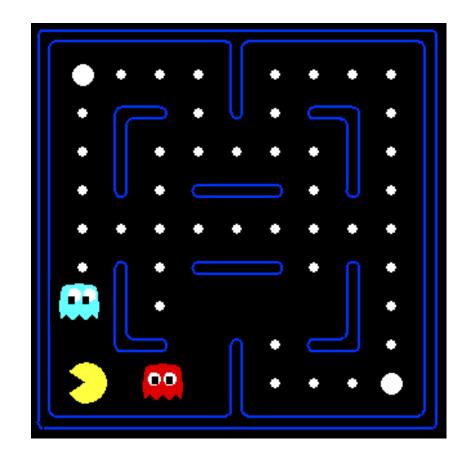
Or even this one!



[Demo: Q-learning – pacman – tiny – watch all (L11D5)] [Demo: Q-learning – pacman – tiny – silent train (L11D6)] [Demo: Q-learning – pacman – tricky – watch all (L11D7)]

#### **Feature-Based Representations**

- Solution: describe a state using a vector of features (properties)
  - Features are functions from states to real numbers (often 0/1) that capture important properties of the state
  - Example features:
    - Distance to closest ghost
    - Distance to closest dot
    - Number of ghosts
    - 1 / (dist to dot)<sup>2</sup>
    - Is Pacman in a tunnel? (0/1)
    - ..... etc.
    - Is it the exact state on this slide?
  - Can also describe a q-state (s, a) with features (e.g. action moves closer to food)



#### **Linear Value Functions**

 Using a feature representation, we can write a q function (or value function) for any state using a few weights:

$$V(s) = w_1 f_1(s) + w_2 f_2(s) + \ldots + w_n f_n(s)$$

$$Q(s,a) = w_1 f_1(s,a) + w_2 f_2(s,a) + \ldots + w_n f_n(s,a)$$

- Advantage: our experience is summed up in a few powerful numbers
- Disadvantage: states may share features but actually be very different in value!

## **Approximate Q-Learning**

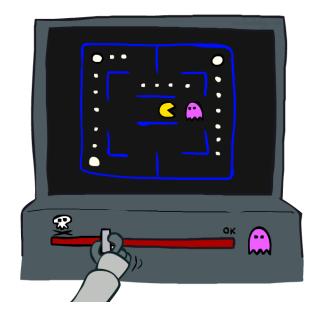
$$Q(s,a) = w_1 f_1(s,a) + w_2 f_2(s,a) + \ldots + w_n f_n(s,a)$$

Q's

Q-learning with linear Q-functions:

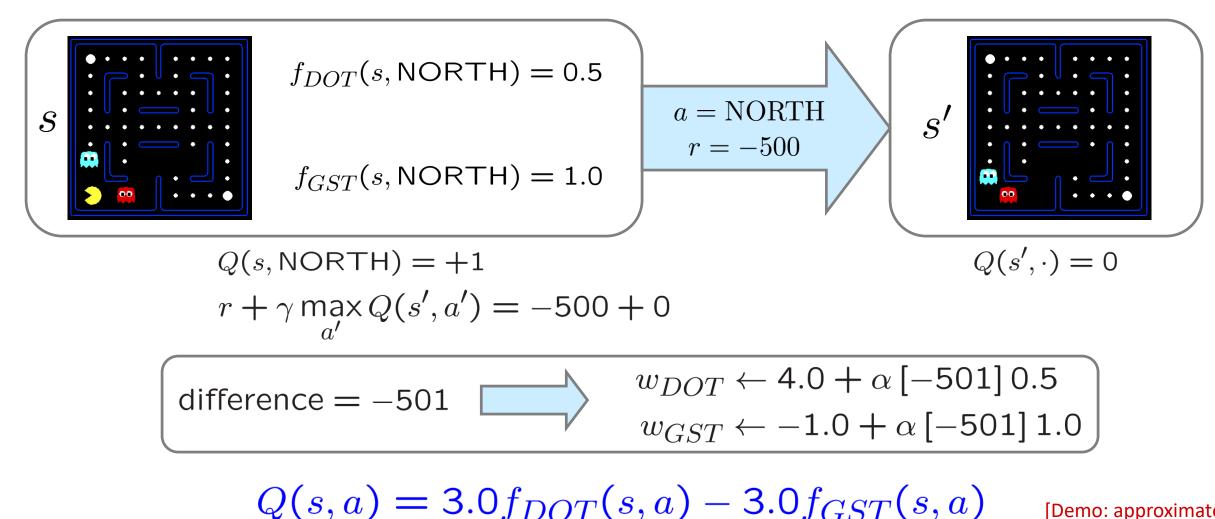
transition = 
$$(s, a, r, s')$$
  
difference =  $\left[r + \gamma \max_{a'} Q(s', a')\right] - Q(s, a)$   
 $Q(s, a) \leftarrow Q(s, a) + \alpha$  [difference] Exact Q's  
 $w_i \leftarrow w_i + \alpha$  [difference]  $f_i(s, a)$  Approximate Q's

- Adjust weights of active features
- E.g., if something unexpectedly bad happens, blame the features that were on: disprefer all states with that state's features
- Formal justification: online least squares



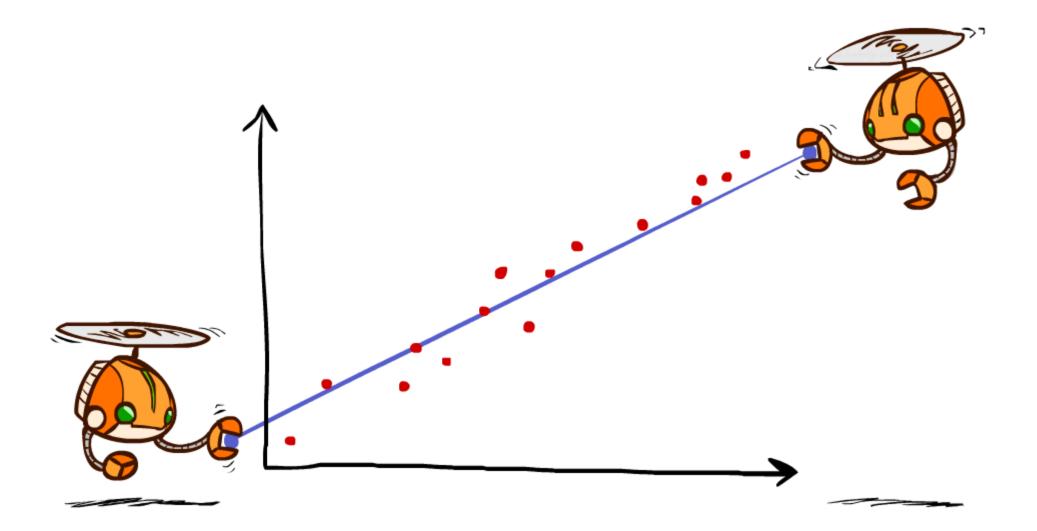
#### Example: Q-Pacman

$$Q(s,a) = 4.0 f_{DOT}(s,a) - 1.0 f_{GST}(s,a)$$

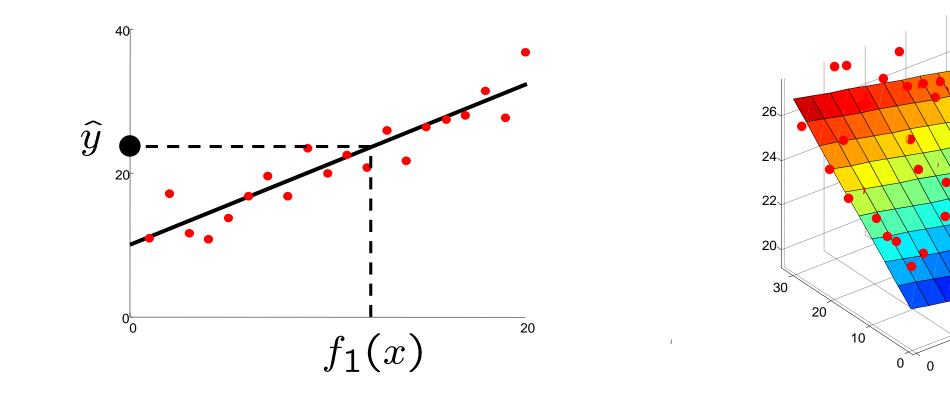


(S, a) [Demo: approximate Qlearning pacman (L11D10)]

#### Q-Learning and Least Squares



#### Linear Approximation: Regression\*



Prediction:  $\hat{y} = w_0 + w_1 f_1(x)$  Prediction:  $\hat{y}_i = w_0 + w_1 f_1(x) + w_2 f_2(x)$ 

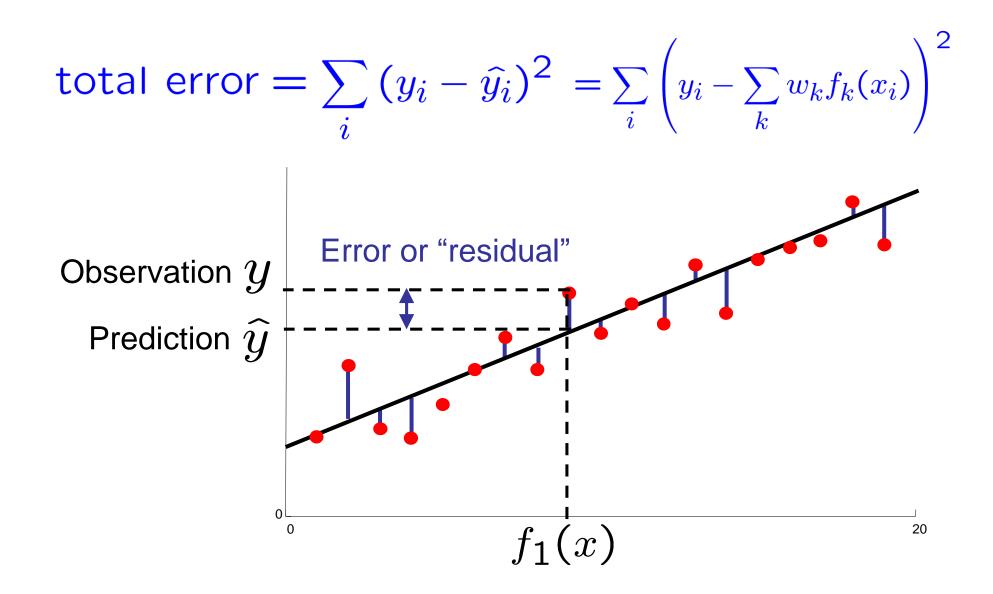
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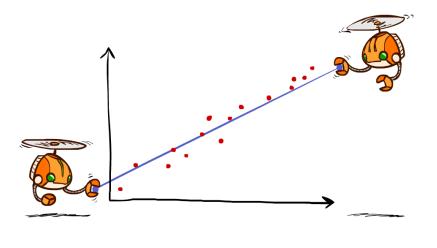
#### **Optimization:** Least Squares\*



### Minimizing Error\*

Imagine we had only one point x, with features f(x), target value y, and weights w:

$$\operatorname{error}(w) = \frac{1}{2} \left( y - \sum_{k} w_{k} f_{k}(x) \right)^{2}$$
$$\frac{\partial \operatorname{error}(w)}{\partial w_{m}} = - \left( y - \sum_{k} w_{k} f_{k}(x) \right) f_{m}(x)$$
$$w_{m} \leftarrow w_{m} + \alpha \left( y - \sum_{k} w_{k} f_{k}(x) \right) f_{m}(x)$$



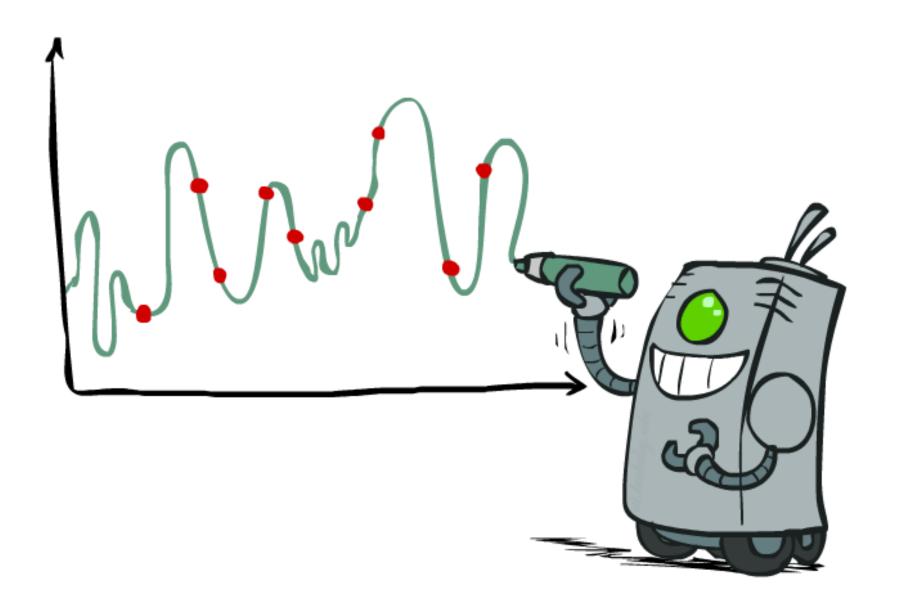
Approximate q update explained:

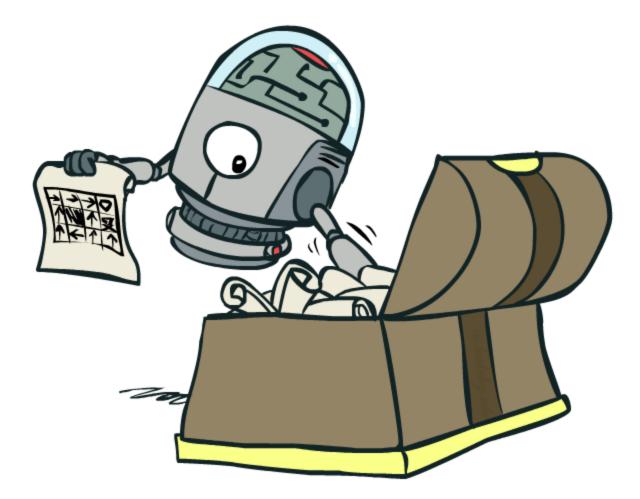
$$w_m \leftarrow w_m + \alpha \left[ r + \gamma \max_a Q(s', a') - Q(s, a) \right] f_m(s, a)$$

"prediction"

"target"

#### **Overfitting: Why Limiting Capacity Can Help\***





- Problem: often the feature-based policies that work well (win games, maximize utilities) aren't the ones that approximate V / Q best
  - E.g. your value functions from project 2 were probably horrible estimates of future rewards, but they still produced good decisions
  - Q-learning's priority: get Q-values close (modeling)
  - Action selection priority: get ordering of Q-values right (prediction)
  - We'll see this distinction between modeling and prediction again later in the course
- Solution: learn policies that maximize rewards, not the values that predict them
- Policy search: start with an ok solution (e.g. Q-learning) then fine-tune by hill climbing on feature weights

- Simplest policy search:
  - Start with an initial linear value function or Q-function
  - Nudge each feature weight up and down and see if your policy is better than before
- Problems:
  - How do we tell the policy got better?
  - Need to run many sample episodes!
  - If there are a lot of features, this can be impractical
- Better methods exploit lookahead structure, sample wisely, change multiple parameters...



#### [Andrew Ng]

#### [Video: HELICOPTER]

## Conclusion

- We're done with Part I: Search and Planning!
- We've seen how AI methods can solve problems in:
  - Search
  - Constraint Satisfaction Problems
  - Games
  - Markov Decision Problems
  - Reinforcement Learning
- Next up: Part II: Uncertainty and Learning!



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